

M. Hrušák and D. M. Alcántara introduced a Wadge-like game: Let  $\mathcal{I}$  and  $\mathcal{J}$  be two Borel ideals on  $\omega$ . The *Comparison game* for  $\mathcal{I}$  and  $\mathcal{J}$  denoted by  $G(\mathcal{I}, \mathcal{J})$  plays as follows: In step  $n$ , Player I plays  $I_n \in \mathcal{I}$ , Player II play  $J_n \in \mathcal{J}$ , Player II wins if  $\bigcup_{n \in \omega} I_n$  iff  $\bigcup_{n \in \omega} J_n \in \mathcal{J}$ . If Player II has a winning strategy, we denote  $\mathcal{I} \sqsubseteq \mathcal{J}$ . We say that  $\mathcal{I} \simeq \mathcal{J}$  if  $\mathcal{I} \sqsubseteq \mathcal{J}$  and  $\mathcal{J} \sqsubseteq \mathcal{I}$ .

In this talk we will brief introduce some known properties of Comparison game, and then answer some questions asked by M. Hrušák and D. M. Alcántara list below:

- Is the order  $\sqsubseteq$  linear (a well order)?
- Are there exactly two class of  $F_{\sigma\delta}$  non  $F_\sigma$ -ideals?
- How many classes of  $F_{\sigma\delta\sigma}$ -ideals are there?

To answer these questions, we define a operator on Borel ideal by  $T(\mathcal{I})$  is the ideal on  ${}^{<\omega}2$  generated by  $\{\{x|n : n \in \omega\} : x \in \mathcal{I}\}$ . The main result as follows: If  $\mathcal{I}, \mathcal{J}$  be two Borel ideals which above  $D_\omega(\Sigma_2^0)$ , then  $\mathcal{I} \equiv_W \mathcal{J} \Leftrightarrow T(\mathcal{I}) \simeq T(\mathcal{J})$ .

#### REFERENCES

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3. A. S. Kechris, *Classical Descriptive Set Theory*, Graduate Texts in Mathematics 156, Springer-Verlag, 1995.