CICHOŃ'S MAXIMUM WITH EVASION NUMBER

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Abstract

For a long time it had been an open problem whether all the cardinal invariants in Cichoń's diagram can be separated simultaneously (except for the two dependent numbers $\operatorname{add}(\mathcal{M})$ and $\operatorname{cof}(\mathcal{M})$), until it was positively solved recently by the construction of such a simultaneous separation model, which is called Cichoń's maximum. The aim of our study is to add other cardinal invariants to Cichoń's maximum and we focus on the evasion number \mathfrak{e} . We show that \mathfrak{e} can be added to Cichoń's maximum with a distinct value in the following order $\aleph_1 < \operatorname{add}(\mathcal{N}) < \operatorname{cov}(\mathcal{N}) < \mathfrak{b} < \mathfrak{e} < \operatorname{non}(\mathcal{M}) < \operatorname{cov}(\mathcal{M}) < \mathfrak{d} < \operatorname{non}(\mathcal{N}) < \operatorname{cof}(\mathcal{N}) < 2^{\aleph_0}$.