(Non)measurability of $\mathcal{I}$-Luzin sets

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For reasonable σ-ideal of sets we call a set A an $\mathcal{I}$-Luzin sets if for every $I \in \mathcal{I}$ we have $|A \cap I| < |A|$. If such a set intersects each Borel $\mathcal{I}$-positive set on a set of the same cardinality, then we have super $\mathcal{I}$-Luzin set. Such a notion generalizes classic notion of Luzin sets and Sierpiński sets on the real line (or Euclidean space). We will give necessary and sufficient condition for $\mathcal{I}$-nomeasurability of $\mathcal{I}$-Luzin sets and, using the Smital Property (precisely- its weaker version), we will provide an easy way to generate super $\mathcal{I}$-Luzin sets ($\mathcal{I}$-Luzin sets that) if only $\mathcal{I}$-Luzin sets exist. As a final result we shall show that if $\mathfrak{c}$ is a regular cardinal and L is a generalized Luzin set and S- a generalized Sierpiński set, then their algebraic sum $L + S$ belongs to the Marczewski ideal s_0.